

## FORMULATION OF MEMBER STIFFNESS MATRIX FOR BEAM

$$\begin{array}{cccc}
 \mathbf{V} & \mathbf{R} & \mathbf{V} & \mathbf{R} \\
 \left. \begin{array}{l} 12EI/L^3 \\ 6EI/L^2 \\ -12EI/L^3 \\ 6EI/L^2 \end{array} \right\} & \begin{array}{l} 6EI/L^2 \\ 4EI/L \\ -6EI/L^2 \\ 2EI/L \end{array} & \left. \begin{array}{l} -12EI/L^3 \\ -6EI/L^2 \\ 12EI/L^3 \\ -6EI/L^2 \end{array} \right\} & \begin{array}{l} 6EI/L^2 \\ 2EI/L \\ -6EI/L^2 \\ 4EI/L \end{array} \\
 & & & \left. \begin{array}{l} \mathbf{V} \\ \mathbf{R} \\ \mathbf{V} \\ \mathbf{R} \end{array} \right\}
 \end{array}$$

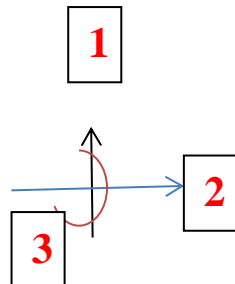
### SIMPLIFIED FORM

TAKE EI/L AS COMMON FROM BRACKET

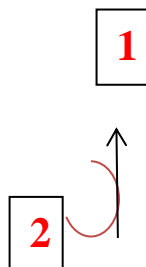
$$\left[ \begin{array}{cccc}
 12/L^2 & 6/L & -12/L^2 & 6/L \\
 6/L & 4 & -6/L & 2 \\
 -12/L^2 & -6/L & 12/L^2 & -6/L \\
 6/L & 2 & -6/L & 4
 \end{array} \right]$$

### STEP BY STEP PROCEDURE FOR ANALYSIS OF BEAM USING DIRECT STIFFNESS METHOD

- 1) IDENTIFICATION OF DOKI (DEGREE OF KINEMATIC INDETERMINANCY) FROM FIG.
- 2) MARKING OF UNKNOWN AND KNOWN DOF AT EACH NODAL POINT USING SYMBOLS 1, 2, 3 ETC
- 3) REMEMBER, ALWAYS START WRITING THE SYMBOLS WITH UNKNOWN DOF FIRST THEN KNOWN DOF AND IN THAT REPRESENTATION IS LIKE THIS



ALSO AS IN BEAM AXIAL DEFORMATION IS NEGLECTED SO SYMBOL 2 WILL BE SKIPPED THEN WE WILL GET



4) FORMULATION OF MEMBER STIFFNESS MATRIX FOR BEAM OF 2 NODAL POINTS AT A TIME.

$$\begin{array}{cccc}
 \mathbf{V} & \mathbf{R} & \mathbf{V} & \mathbf{R} \\
 \left. \begin{array}{l} 12EI/L^3 \\ 6EI/L^2 \\ -12EI/L^3 \\ 6EI/L^2 \end{array} \right\} & \begin{array}{l} 6EI/L^2 \\ 4EI/L \\ -6EI/L^2 \\ 2EI/L \end{array} & \left. \begin{array}{l} -12EI/L^3 \\ -6EI/L^2 \\ 12EI/L^3 \\ -6EI/L^2 \end{array} \right\} & \begin{array}{l} 6EI/L^2 \\ 2EI/L \\ -6EI/L^2 \\ 4EI/L \end{array} \\
 & & & \left. \begin{array}{l} \mathbf{V} \\ \mathbf{R} \\ \mathbf{V} \\ \mathbf{R} \end{array} \right\}
 \end{array}$$

**SIMPLIFIED FORM**

**TAKE EI/L AS COMMON FROM BRACKET**

$$\left[ \begin{array}{cccc}
 12/L^2 & 6/L & -12/L^2 & 6/L \\
 6/L & 4 & -6/L & 2 \\
 -12/L^2 & -6/L & 12/L^2 & -6/L \\
 6/L & 2 & -6/L & 4
 \end{array} \right]$$

5) FORMULATION OF GLOBAL STIFFNESS MATRIX

K MATRIX BASED ON UNKOWN DOF

6) CALCULATION OF GLOBAL LOAD MATRIX

7) DISPLACEMENT CALCULATION

$$(\mathbf{K})(\mathbf{D.F}) = (\mathbf{A.F.C})$$

8) CALCULATION OF FINAL MEMBER FORCES

$$(\mathbf{A.M}) = (\mathbf{AML}) + (\mathbf{SM})(\mathbf{D.M})$$

9) PLOTTING OF BMD AND SFD